

# Automatic Compositional Verification of Timed Systems (Tool Paper)

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# Motivation

State Space Explosion Problem w.r.t. Model Checking

Assume-Guarantee Reasoning (AGR)

$$\frac{M_1 \parallel A \models \varphi \quad M_2 \models A}{M_1 \parallel M_2 \models \varphi}$$

How to construct the assumption  $A$  *automatically*?

- ▶ Untimed systems
  - ▶ J. M. Cobleigh, D. Giannakopoulou, and C. S. Păsăreanu. Learning assumptions for compositional verification. In TACAS, volume 2619 of LNCS, pp. 331–346, 2003.
- ▶ How about *timed systems*?

# Outline

Event-Recording Automata (ERA)

The TL\* Algorithm

Learning-Based Automatic Compositional Verification

Experiment Results

Conclusion and Future Work

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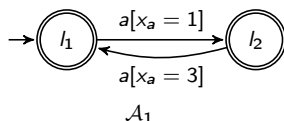
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# Event-Recording Automata (ERA)

The following ERA  $\mathcal{A}_1$  accepts the timed language  $U_T^{\mathcal{A}_1}$  of the form  $(a, t_1)(a, t_2)(a, t_3) \cdots$  where  $t_{2i} - t_{2i-1} = 3$  and  $t_{2i+1} - t_{2i} = 1$  for all  $i \geq 1$

- ▶  $(a, 1)(a, 4)$
- ▶  $(a, 1)(a, 4)(a, 5)(a, 8)(a, 9)$



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# The TL\* Algorithm

The TL\* algorithm is a *timed* extension of the L\* algorithm.

The TL\* algorithm is a formal method to learn a minimal event-recording automaton (ERA) that accepts an *unknown timed language*  $U_T$  over an alphabet  $\Sigma$

- ▶ We use  $U$  to denote the *untimed language* of  $U_T$

## The TL\* Algorithm (cont.)

The TL\* algorithm has to interact with a Minimal Adequate *Teacher*

- ▶ *untimed membership query*  $Q_m$ 
  - ▶ Is an untimed word in the unknown untimed language  $U$ ?
- ▶ *untimed candidate query*  $Q_c$ 
  - ▶ Does a DFA accept the unknown untimed language  $U$ ?
- ▶ *timed membership query*  $Q_m^T$ 
  - ▶ Is a guarded word in the unknown timed language  $U_T$ ?
- ▶ *timed candidate query*  $Q_c^T$ 
  - ▶ Does an ERA accept the unknown timed language  $U_T$ ?



# The TL\* Algorithm (cont.)

The TL\* algorithm consists of two phases

- ▶ *Untimed Learning* Phase
  - ▶ The L\* algorithm is used to learn a DFA  $M$  accepting the untimed language  $U$
- ▶ *Timed Refinement* Phase
  - ▶ The DFA  $M$  is **refined** into an event-recording automaton (ERA) by adding **time constraints** or **locations**

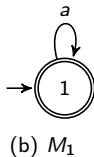
# An Example

Suppose  $U_T^{A_1}$  is the timed language to be learned.

Untimed Learning Phase

	$\lambda$
$\lambda$	1 ( $s_0$ )
$a$	1

(a)  $T_1$



	$\lambda$
$\lambda$	1 ( $s_0$ )
$(a, true)$	1

(c)  $T_2$

$$\mathcal{L}(M_1) = U^{A_1} = a^*$$

## An Example (cont.)

$Q_c^T(M_1) = 0$  with a negative counterexample  $(a, x_a < 1)$

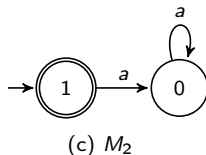
Timed Refinement 1

$\lambda$	$\lambda$
	1 ( $s_0$ )
$(a, x_a < 1)$	0
$(a, x_a \geq 1)$	0

(a)  $T_3$

$\lambda$	$\lambda$
	1 ( $s_0$ )
$(a, x_a < 1)$	0 ( $s_1$ )
$(a, x_a \geq 1)$	0
$(a, x_a < 1)(a, x_a < 1)$	0
$(a, x_a < 1)(a, x_a \geq 1)$	0

(b)  $T_4$



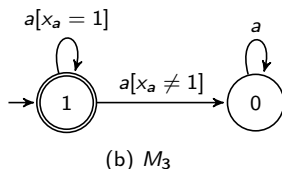
## An Example (cont.)

$Q_c^T(M_2) = 0$  with a positive counterexample  $(a, x_a = 1)$

### Timed Refinement 2

	$\lambda$
$\lambda$	1 ( $s_0$ )
$(a, x_a < 1)$	0 ( $s_1$ )
$(a, x_a = 1)$	1
$(a, x_a > 1)$	0
$(a, x_a < 1)(a, x_a < 1)$	0
$(a, x_a < 1)(a, x_a = 1)$	0
$(a, x_a < 1)(a, x_a > 1)$	0

(a)  $T_5$



## An Example (cont.)

$Q_c^T(M_3) = 0$  with a negative counterexample  $(a, x_a = 1)(a, x_a = 1)$

A suffix  $(a, x_a = 1)$  shows that  $\lambda$  and  $(a, x_a = 1)$  should not be in the same class

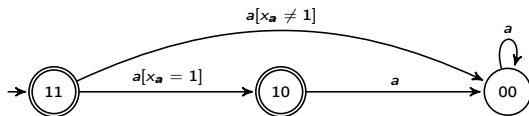
### Timed Refinement 3

	$\lambda$	$(a, x_a = 1)$
$\lambda$	1	1 ( $s_0$ )
$(a, x_a < 1)$	0	0 ( $s_1$ )
$(a, x_a = 1)$	1	0
$(a, x_a > 1)$	0	0
$(a, x_a < 1)(a, x_a < 1)$	0	0
$(a, x_a < 1)(a, x_a = 1)$	0	0
$(a, x_a < 1)(a, x_a > 1)$	0	0

(a)  $T_6$

	$\lambda$	$(a, x_a = 1)$
$\lambda$	1	1 ( $s_0$ )
$(a, x_a < 1)$	0	0 ( $s_1$ )
$(a, x_a = 1)$	1	0 ( $s_2$ )
$(a, x_a > 1)$	0	0
$(a, x_a < 1)(a, x_a < 1)$	0	0
$(a, x_a < 1)(a, x_a = 1)$	0	0
$(a, x_a < 1)(a, x_a > 1)$	0	0
$(a, x_a = 1)(a, x_a < 1)$	0	0
$(a, x_a = 1)(a, x_a = 1)$	0	0
$(a, x_a = 1)(a, x_a > 1)$	0	0

(b)  $T_7$



(c)  $M_4$

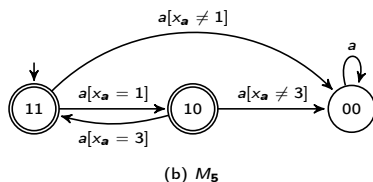
## An Example (cont.)

$Q_c^T(M_4) = 0$  with a positive counterexample  $(a, x_a = 1)(a, x_a = 3)$

### Timed Refinement 4

$\lambda$	$\lambda$	$(a, x_a = 1)$
	1	1 ( $s_0$ )
$(a, x_a < 1)$	0	0 ( $s_1$ )
$(a, x_a = 1)$	1	0 ( $s_2$ )
$(a, 1 < x_a < 3)$	0	0
$(a, x_a = 3)$	0	0
$(a, x_a > 3)$	0	0
$(a, x_a < 1)(a, x_a < 1)$	0	0
$(a, x_a < 1)(a, x_a = 1)$	0	0
$(a, x_a < 1)(a, 1 < x_a < 3)$	0	0
$(a, x_a < 1)(a, x_a = 3)$	0	0
$(a, x_a < 1)(a, x_a > 3)$	0	0
$(a, x_a = 1)(a, x_a < 1)$	0	0
$(a, x_a = 1)(a, x_a = 1)$	0	0
$(a, x_a = 1)(a, 1 < x_a < 3)$	0	0
$(a, x_a = 1)(a, x_a = 3)$	1	1
$(a, x_a = 1)(a, x_a > 3)$	0	0

(a)  $T_8$



## An Example (cont.)

$$Q_c^T(M_5) = \mathbf{1}, \text{ i.e., } \mathcal{L}(M_5) = U_T^{A_1}$$

The learning process of  $TL^*$  is finished

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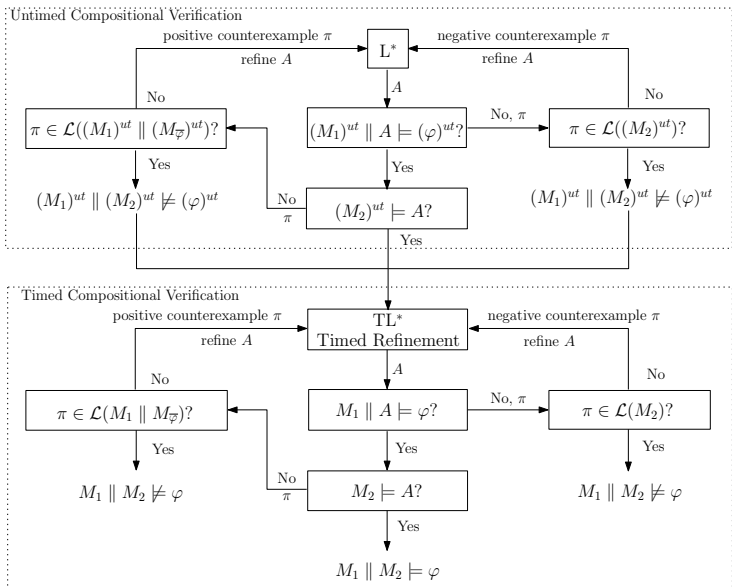
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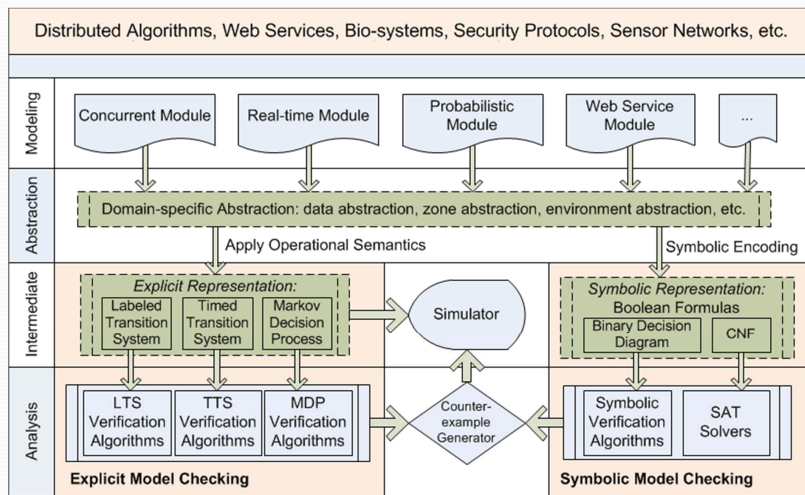
Conclusion and Future Work



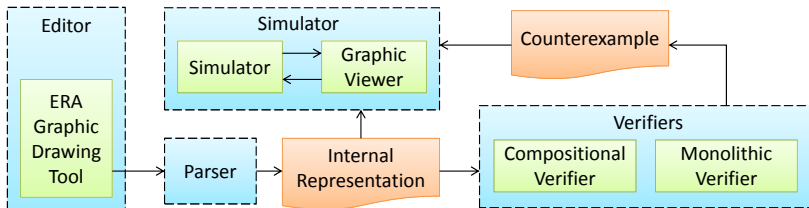
# Overall Flow



# Architecture of Process Analysis Toolkit (PAT)



# The ERA Module



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# Experiment Results

**Table 1.** Verification Results

System	$n$	$ C_{\Sigma} $	$ P_{\neq} $		Monolithic				Compositional				UPPAAL
			$ P $	$ L _{max}$	$ \delta _{max}$	Time (secs)	Mem (MB)	$ L _{max}$	$ \delta _{max}$	Time (secs)	Mem (MB)	Time (secs)	
CSS	3	6	0/6	11	20	0.03	0.16	19	50	0.06	0.77	0.05	
GSS	3	3	2/3	29	46	0.03	0.13	56	107	0.03	0.69	0.06	
FMS-1	5	3	1/3	193	514	0.03	1.18	60	138	0.03	0.89	0.08	
FMS-2	10	6	3/6	76,305	396,789	40.71	114.08	1,492	4,952	0.66	6.60	2.05	
FMS-3	11	6	5/7	201,601	1,300,566	70.02	295.89	3,150	16,135	1.14	12.07	9.87	
FMS-4	14	8	3/9	—	—	—	ROM	26,320	127,656	51.02	41.41	ROM	
AIP	10	4	5/10	104,651	704,110	78.05	149.68	2,992	12,971	1.90	7.39	N/A	

$n$ : # of components;  $|C_{\Sigma}|$ : # of event-recording clocks;  $|P|$ : # of properties;  $|P_{\neq}|$ : # of violated properties;  $|L|_{max}$ : # of visited locations during verification;  $|\delta|_{max}$ : # of visited transitions during verification; ROM: run out of memory

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We propose

- ▶ a learning algorithm,  $TL^*$ , for ERAs
- ▶ a learning-based compositional verification for timed systems modeled by ERAs

In the future, we plan to

- ▶ use different techniques to generate the assumptions
- ▶ use different proof rules for AGR